

1 Cycling Time Trial Strategies Considering Peak Power-Time Curve and Acceleration

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10

11 **ABSTRACT**

12 The constant power pacing strategy is typically recommended for long, flat, and windless cycling time trial races.
13 For courses with wind or hills, a variable power pacing strategy is often suggested—one that increases power during
14 headwind or uphill sections and decreases it during tailwind or downhill sections. We analyzed 10 km and 1 km
15 courses under various conditions, including flat and windless, windy, and hilly scenarios, and compared different
16 pacing strategies by considering peak power–time curves and acceleration. For 10 km courses, a fast-start strategy
17 followed by constant power was found to be effective. In contrast, the variable power pacing strategy showed no
18 significant advantage and even worsened finish times when the course started with a downhill followed by an uphill
19 section. For 1 km courses, the variable power pacing strategy improved performance except for the tailwind-then-
20 headwind scenario, where it actually worsened the finish time. In contrast to 10 km courses, the downhill-then-
21 uphill case saw a marked improvement with the variable power pacing approach.

22

23 Keywords: Cycling time trial; Peak power-time curve; Acceleration; Simulation, Variable power pacing strategy

24

25 **1. Introduction**

26 Power management is critical to success in cycling time trial races. Several studies have demonstrated that a variable
27 power pacing strategy—characterized by increasing power output during headwinds and uphill sections, and
28 reducing it during tailwinds and downhill segments—can significantly reduce race times on realistic courses.¹⁻⁶

29
30 Among these studies, Cangley et al. (2011) specifically validated the uphill and downhill aspects of this strategy
31 through field experiments on a hilly course.⁴ While their results confirmed the potential for time savings, the actual
32 improvement observed was smaller than that predicted by simulations. A key reason was that some participants
33 struggled to sustain the increased power required during uphill sections.

34
35 In actual time trial races, riders adopting a constant power pacing strategy typically aim to maintain the highest
36 power they can manage throughout the race. If however, they increase their power output during uphill segments
37 or headwinds, they risk early fatigue, which may prevent them from sustaining their effort to the finish.

38
39 Therefore, it is essential to consider the relationship between power output and the duration for which a rider can
40 sustain it in order to produce more realistic simulations. Gordon (2005) simulated 40-km cycling time trials by
41 incorporating exertion based on the peak power–time curve.⁷ He calculated optimal power distributions and
42 corresponding finishing times for scenarios such as uphill-then-downhill and headwind-then-tailwind courses. On
43 a course featuring a single climb followed by a descent, the variable power pacing strategy was found to be
44 infeasible due to exertion constraints. However, significant performance gains were demonstrated on courses
45 consisting of repeated 1-km climbs and 1-km descents. In contrast, varying power output for headwind-then-
46 tailwind scenarios yielded no meaningful advantage.

47
48 Dahmen et al. (2012) simulated a 4-km uphill time trial with a constant gradient, as well as a 3.6-km uneven uphill
49 course simulating the Schienerberg, taking into account both exertion and acceleration.⁸ They mathematically
50 optimized the power profiles. For constant-gradient slopes, they showed that the optimal profile involved high
51 power at the beginning and decreasing toward the end for a 1% slope, while for a 10% slope, the optimal profile
52 involved slightly reduced power both at the beginning and the end. For the uneven slope, they demonstrated that a
53 rider following a power profile optimized for time could reduce finishing time without increasing exertion, and that
54 following a profile optimized for exertion could reduce effort while maintaining the same finishing time, compared

55 to an unregulated (free) ride. However, their study did not include a comparison with the constant power pacing
56 strategy.

57
58 Short time trial courses of around 1 km are common in track cycling, and local amateur races are sometimes
59 similarly short and hilly. Wilberg and Pratt (1988) analyzed lap times of 1-km and 3-km race winners in world-
60 class competitions and identified optimal pacing profiles.⁹ In 3-km races, the first lap (333.33 m) was slower than
61 the mean lap time (MLT), while the second lap was the fastest. From the third to sixth laps, lap times remained
62 below the MLT. The seventh lap was approximately equal to the MLT, and the remaining laps were slower. In 1-
63 km races, the first lap was slower than the MLT, the second lap faster, and the final lap again slower than the MLT.

64
65 These findings suggest that in short time trials, an initial increase in power to rapidly reach top speed—followed
66 by an attempt to maintain that speed, albeit with some decline—is an effective pacing strategy. Moreover,
67 comparisons with optimal pacing profiles revealed that riders who accelerated too aggressively early on were
68 ultimately outperformed by those who paced themselves more evenly. This highlights the need to determine,
69 through simulation, an appropriate level of initial power output that balances acceleration demands with sustainable
70 exertion, accounting for the peak power–time relationship.

71
72 Although acceleration plays a crucial role in short-distance time trials, it has been largely overlooked in prior
73 research on longer events, with a few notable exceptions.^{5, 6, 8, 10}

74
75 In this study, we developed a program to simulate cycling time trial performance while incorporating both exertion
76 based on the peak power–time curve and the effects of acceleration. We evaluated the effectiveness of different
77 power variation pacing strategies, including an initial sprint. Although no sophisticated optimization techniques
78 were used, we aimed to identify simple and practical pacing strategies that cyclists can realistically adopt, rather
79 than relying on precisely optimized power profiles tailored to specific course characteristics.

80
81 **2. Methods**
82 The acceleration a of the cycle and rider, with a total mass of m and M , respectively is represented as:

83
$$a = \frac{F}{M + m + m'}. \quad (1)$$

84 The resultant force F is given by:

85
$$F = F_D - F_A - F_R - F_G \quad (2)$$

86 The driving force F_D generated by pedaling is:

87
$$F_D = \frac{f_p}{R_G} \frac{L}{r_w} \quad (3)$$

88 where f_p is the pedaling force, R_G is the gear ratio, L is the crank length, and r_w is the wheel radius. The air drag F_A is expressed as:

90
$$F_A = \frac{1}{2} \rho C_D A v_R^2 \quad (4)$$

91 where v_R is the relative speed, ρ is the air density, C_D is the drag coefficient, and A is the projected frontal area. The 92 rolling resistance F_R is:

93
$$F_R = C_R (M + m)g \quad (5)$$

94 where C_R is the rolling resistance coefficient and g is the gravitational acceleration. The gravity force component 95 along the slope F_G is:

96
$$F_G = (M + m)g \sin \theta \quad (6)$$

97 where θ is the slope angle, and $\tan \theta$ represents the gradient. Only headwinds and tailwinds were considered in this 98 model. Inclined winds and the associated sailing effect were excluded. Additionally, frictional losses from the chain 99 and bearings were ignored. The virtual mass m' , according to the wheels' moment of inertia I is defined as:

100
$$m' = \frac{I}{r_w^2} \quad (7)$$

101 Human output power P is calculated as:

102
$$P = f_p \omega L \quad (8)$$

103 where ω is the angular velocity of the crank.

104

105 For the relationship between P and maximum duration t_c , the 3-parameter critical power model by Morton (1966) 106 was adopted:

107
$$t_c = AWC \left(\frac{1}{P - P_c} - \frac{1}{P_{\max} - P_c} \right) \quad (9)$$

108 where AWC is the anaerobic work capacity, P_c is the critical power (the asymptotic power for infinite duration), 109 and P_{\max} is the maximum power (where t_c becomes zero).¹¹ Cumulative anaerobic work AW for varying power can

110 be calculated as:

$$111 \quad AW = \sum_{i=1}^n \frac{(P_i - P_C)(P_{\max} - P_C)}{(P_{\max} - P_i)} \Delta t \quad (10)$$

112 for a data series at t_i , ($i = 1, 2, \dots, n$), with a time interval of Δt . The exertion E is defined as

$$113 \quad E = \frac{AW}{AWC} \quad (12)$$

114 (Gordon, 2005).⁷ It is assumed that the rider is no longer able to sustain the required power level when $E = 1$.

115 Recovery occurs when $P < P_C$, leading to a decrease in AW. However, E immediately reaches 1 if P reaches P_{\max} .

116

117 The parameters AWC, P_{\max} and P_C in Eq. (9) can be calculated using at least three, preferably four or more, average
118 power-maximum duration data points. Many serious cyclists today utilize power meters and web-based analysis
119 tools to create their own power profiles. By substituting multiple pairs of duration and peak power data from an
120 amateur male cyclist (62 years old, 171 cm, and 59 kg) into Eq. (9), the parameters AWC, P_{\max} , and P_C can be
121 derived. For instance, the solver function in Microsoft Excel can be employed for this task. Assuming the obtained
122 AWC = 9267 J, P_{\max} = 1075 W, and P_C = 252 W, the resulting power profile is illustrated in Fig. 1. These parameters
123 will be used for subsequent calculations.

124

125 The other parameters used in the simulation are listed in Table 1. These values lie within typical ranges and are not
126 customized for specific riders or equipment. Changes in temperature and air pressure were not considered. The
127 simulation proceeded as follows.

128

129 (1) Initial values are assigned to variables.

130 (2) The pedaling force is calculated for the given power. An upper limit of Mg is imposed on the pedaling force,
131 which is typically active at low velocities during the start. As a result, the power may not reach the target value
132 in the early stage.

133 (3) The resultant force is calculated, followed by the acceleration.

134 (4) The velocity v at the time step i is calculated using:

$$135 \quad v_i = v_{i-1} + \frac{a_{i-1} + a_i}{2} \Delta t. \quad (11)$$

136 (5) Distance x at the time step i is calculated as:

137
$$x_i = x_{i-1} + \frac{v_{i-1} + v_i}{2} \Delta t. \quad (12)$$

138 (6) Exertion is calculated. Exertion is set to 0 when AW becomes negative, particularly at the start.

139 (7) Steps (2) to (6) are repeated, incrementing i .

140
141 The simulations focused on 10 km and 1 km time trial races. For the 10 km simulations, the time step Δt was set to
142 10 ms. However, for the 1 km simulations, a smaller time step of 1 ms was used, as preliminary calculations revealed
143 that a 10 ms interval was not sufficiently small to ensure accurate results.

144
145 **3. Results and discussion for the 10 km case**
146 **3.1 Windless and flat course**
147 A windless and flat 10 km course was simulated. First, the constant power pacing strategy was analyzed. The
148 maximum constant power that allowed the rider to complete the 10 km distance without exceeding an exertion level
149 of 1 was determined by a trial-and-error method with a resolution of 0.1 W. The optimal power was found to be
150 262.6 W, resulting in a completion time of 857.99 seconds (Fig. 2, 10C in Table 2). At power levels below this, the
151 completion time increased, while at higher power levels, the rider could not finish the course due to excessive
152 fatigue.

153
154 Next, power variation pacing strategies were investigated. In the first scenario, power output was increased during
155 the first half of the course. The maximum power sustained over the initial 5 km was determined to be 273.0 W.
156 Although the rider could maintain the critical power level (252 W) needed to complete the race, the finishing time
157 was 858.43 seconds (10IDmax; "max" refers to the maximum value sustained during the first half), which was 0.44
158 seconds slower than the constant power pacing strategy. This indicates that the slight advantage gained by faster
159 acceleration at the start was insufficient to offset the overall increase in fatigue.

160
161 In the second scenario, power during the first half of the course was decreased by the same amount of 10.4 W, with
162 a corresponding increase in the second half raising the maximum power to 273.4 W. This resulted in a completion
163 time of 858.69 seconds (10DI), which was slightly slower than the constant power pacing strategy.

164
165 The effects of a start sprint were also analyzed, as time trial riders often produce higher power outputs at the

166 beginning of a race than during steady cruising. Starting powers ranging from 200 to 500 W over the first 5 seconds
167 were tested. The results showed that a starting power of 400 W improved the finish time by 1.01 seconds (10S+137.4,
168 Table 3), whereas higher starting powers, such as 500 W (10S+237.4), reduced the cruising power and worsened
169 overall performance. Conversely, starting power levels below the cruising power also degraded completion times
170 (10S-062.6).

171
172 These findings confirm that a constant power pacing strategy remains fundamentally the most effective approach
173 for a windless and flat 10 km time trial, even when acceleration effects are considered. Although a fast start with a
174 moderate start sprint can yield slight improvements, excessive power output at the start reduces sustainable cruising
175 power and ultimately leads to poorer performance. Since riders frequently apply excessive power unintentionally
176 at the start, careful management of the start sprint is crucial to avoid performance degradation.² To simplify
177 subsequent analyses and isolate the effects of other variables, the start sprint was excluded in further simulations.
178

179 **3.2 Flat but windy course**

180 The effects of wind conditions on time trial performance were analyzed by simulating cases with headwind and
181 tailwind on a flat 10 km course. In the first scenario, the rider encountered a headwind during the first half and a
182 tailwind in the latter half, with a wind speed of 10 m/s. The constant power pacing strategy resulted in a slightly
183 reduced optimal power of 260.7 W, due to the increased time spent in the headwind section (10HTC, Table 4).
184 When a variable power pacing strategy was employed, the optimal configuration involved increasing power to
185 263.9 W during the headwind section and decreasing it to 252.1 W during the tailwind section (10HTIDmax). This
186 adjustment improved the total time by 3.0 seconds compared to the constant power pacing strategy. In contrast,
187 decreasing the first-half power by the same 3.2 W required increasing the second-half power to 269.1 W (10HTDI),
188 resulting in a finish time 3.6 seconds slower than the constant power pacing strategy.
189

190 The opposite scenario, in which the rider experienced a tailwind in the first half followed by a headwind in the
191 second half, was also simulated (Table 5). The optimal constant power in this case was 260.8 W, and the completion
192 time was significantly shorter than that in the headwind-first scenario—primarily due to the tailwind facilitating
193 initial acceleration. When the first-half power was reduced to the critical power of 252 W, the second-half maximum
194 power could be increased to 264.2 W, yielding a modest time improvement of 0.47 seconds (10THDImin; "min"
195 refers to the minimum power value during the first half). On the other hand, increasing the first-half power by 8.8

196 W reduced the allowable power in the latter half to 257.4 W (10THID), worsening the time by 4.83 seconds.

197

198 Atkinson et al. (2007) proposed that increasing power output during headwinds and decreasing it during tailwinds
199 by equal amounts could reduce race time.³ However, the present findings suggest that such a strategy may be too
200 simplistic in real-world conditions, as it fails to account for human fatigue and exertion limitations.

201

202 **3.3 Uphill and Downhill Course**

203 In the next scenario, the rider encountered a 10% uphill gradient for the first half of the course, followed by a 10%
204 downhill gradient for the second half, with no wind. The slant distance was used instead of the planar distance.
205 Under a constant power pacing strategy, the finish time was significantly worsened due to the increased resistance
206 from gravitational force during the uphill section and from air drag during the downhill section (10UDC, Table 6).
207 The maximum constant power was reduced to 257.1 W because of the prolonged effort, bringing the rider close to
208 their exertion limit. Due to fatigue constraints, the rider could increase uphill power by only 0.7 W from the constant
209 power pacing strategy. Nevertheless, this modest adjustment improved the finish time by 1.8 seconds (10UDID).
210 In contrast, decreasing the uphill power to the critical power of 252 W drastically worsened the time by 30.3 seconds
211 (10UDDImin), highlighting the sensitivity of performance to reduced power on steep inclines.

212

213 The reverse case—starting with a 10% downhill followed by a 10% uphill—was also simulated (10DUC, Table 7).
214 In this configuration, the constant power remained nearly unchanged, but the finish time was substantially shorter
215 compared to the uphill-first scenario. The downhill start allowed the rider to accelerate rapidly and sustain higher
216 speeds into the initial part of the climb. When the power during the downhill section was reduced to the critical
217 power of 252 W, the rider could increase power on the uphill by 0.8 W. This led to a negligible increase in time—
218 only 0.2 seconds (10DUDImin). Conversely, increasing the downhill power by 5.2 W necessitated a reduction in
219 uphill power by 0.7 W from the constant power pacing strategy, which significantly worsened the time by 13.8
220 seconds (10DUID). These results indicate that power distribution in long, hilly time trials requires careful balancing.
221 In particular, reducing power output on steep uphill sections can result in substantial time losses. Understanding
222 this can help cyclists refine their pacing strategies and improve overall performance.

223

224 **4. Results and discussion for the 1 km case**

225 **4.1 Flat and windless course**

226 The maximum constant power that allowed the rider to complete the 1 km course without exceeding the exertion
227 threshold was determined to be 346.9 W (1C, Table 8). When power was increased to 417.0 W for the first half and
228 decreased to 252 W for the second half, the finish time improved by 1.1 seconds (1IDmax8). In contrast, reducing
229 the first-half power by the same 70.1 W and increasing the second-half power to 419.7 W worsened the time by 3.2
230 seconds (1DI). These results suggest that elevated power early in the race—facilitating initial acceleration and
231 higher speeds into the latter half—is particularly beneficial in short time trials (Fig. 3).

232

233 To further investigate time reduction strategies, simulations were conducted in which the power transition point
234 was varied from 100 m to 900 m in 100 m increments, excluding 500 m, which had already been analyzed. For
235 each change point, a range of power levels—from the constant power to the maximum finishable power—was
236 tested, and the configuration yielding the shortest time was selected. As the change point moved closer to the end
237 of the course, the optimal power levels for both segments gradually decreased (Fig. 4). The best overall time was
238 achieved when the power change occurred at 600 m (Fig. 5). This indicates that a short-duration start sprint may
239 not be effective in improving total time.

240

241 These findings suggest that, for windless and flat short time trials, increasing power during the early part of the
242 course generally leads to better finish times—even if it results in a reduced power output later. This supports the
243 conclusion of Wilberg and Pratt (1988).⁹ If using two distinct power levels, the transition point can be set near or
244 slightly after the course midpoint. A gradual tapering of power may yield even better performance, a possibility that
245 will be explored further in Section 4.4.

246

247 **4.2 Flat windy course**

248 Consider the case where the rider encounters a headwind for the first half and a tailwind for the second half of the
249 flat course, with a wind speed set at 10 m/s. The constant power in this case is reduced to 329.1 W (1HTC in Table
250 9) compared to the windless scenario (1C) due to the increased time in the latter portion of the course. The maximum
251 power for the first half was determined to be 370.4 W, while for the latter half, it was found to be 252.0 W
252 (1HTIDmax). This strategy results in a time improvement of 2.2 seconds compared to the constant power scenario
253 (1HTC). On the other hand, when the power for the first half is decreased by the same 41.3 W, the maximum power
254 for the second half increases to 396.9 W (1HTDI), and the time becomes 3.9 seconds slower than the constant
255 power case (1HTC).

256
257 In the opposite scenario, where the rider faces a tailwind in the first half and a headwind in the second half (Table
258 10), the constant power is slightly higher, at 337.3 W (1THC), due to the acceleration gained from the tailwind
259 during the start. In the case where the power for the first tailwind section is decreased by 10% and the power for
260 the latter headwind section is increased (1THDI-10%), the time is 0.5 seconds slower than the constant power case
261 (1THC). This happens because the lack of start acceleration negates the advantage of increased power during the
262 headwind portion. When the power for the first tailwind section is increased by 10% and the power for the second
263 headwind section is decreased by 10% (1THID+10%), the time is only 0.02 seconds slower than the constant power
264 scenario (1THC). This outcome occurs because the reduced power in the latter part of the course is nearly canceled
265 out by the assistance from the start acceleration, due to the increased power in the first section.

266
267 **4.3 Windless hilly course**
268 In the scenario where the rider faces a 10% uphill for the first half and a 10% downhill for the second half of the 1
269 km course without wind, the total time worsens significantly under a constant power pacing strategy (1UDC in
270 Table 12). This is due to the increased resistance from gravity on the uphill and the limited effect of power output
271 on speed during the downhill, where air drag dominates. The constant power is reduced to 304.4 W to reflect the
272 extended finish time. When the power for the uphill section is increased by 12.5 W, the allowable power for the
273 downhill section must be reduced by 52.4 W (1UDIDmax). This trade-off results in a 4.2-second improvement in
274 finish time. Conversely, reducing the uphill power by the same amount leads to a 47.7 W increase in downhill
275 power (1UDDI), but the finish time worsens by 5.2 seconds.

276
277 In the opposite scenario, where the rider descends first and climbs in the second half (1DUC in Table 13), the
278 constant power is higher and the overall time is significantly faster than in the uphill-first case. This is because the
279 downhill start allows the rider to accelerate early and carry speed into the initial uphill section. Reducing the
280 downhill power by 10% increases the available uphill power by 13.5 W and improves the finish time by 2.2 seconds
281 (1DUDI-10%). At the critical downhill power level (1DUDImin), the uphill power increases by 28.7 W, and the
282 finish time improves by 3.4 seconds compared to the constant power case. In contrast, increasing the downhill
283 power by 10% (1DUID+10%) reduces the uphill power by 13.9 W, leading to a 2.5-second worsening in finish
284 time.

285

286 From these results, it can be concluded that on a short hilly course, allocating more power to the uphill segment
287 and less to the downhill segment leads to improved performance. However, it should be noted that the increase in
288 uphill power tends to be much smaller than the corresponding decrease in downhill power, indicating diminishing
289 returns for downhill effort and the importance of conserving energy for climbs.

290

291 **4.4 Linear decrease in power for the windless flat course**

292 Finally, a strategy was tested where the rider's power output decreases linearly from a high starting power to the
293 critical power of 252 W over the entire 1 km distance. The optimal starting power was found to be 425.8 W, resulting
294 in a finish time of 85.704 seconds. This is 1.4 seconds faster than the constant power pacing strategy (1C) and 0.3
295 seconds faster than the best time achieved by the stepwise increase-decrease pacing strategy (1IDmax).

296

297 Figure 6 shows the exertion profiles for each strategy. In the constant power case, exertion rises linearly, indicating
298 that the rider's maximum ability is not fully exploited. The step-decrease pacing strategy causes exertion to peak
299 very early, inducing significant fatigue. In contrast, the linear decreasing pacing strategy results in a gradual increase
300 in exertion. Although fatigue is higher than with constant power, it is less than with the stepwise pacing strategy,
301 leading to the best finish time.

302

303 While there may be faster power-decreasing patterns to explore in future studies, the 1.4-second improvement in a
304 1 km time trial is meaningful. This suggests that dynamically reducing power over distance can enhance
305 performance more effectively than maintaining constant power.

306

307 **5. Conclusions**

308 The effects of variable power pacing strategies were investigated through numerical simulations that considered
309 the peak power-time relationship and acceleration. The main findings for 10 km time trials are summarized as
310 follows:

311

312 (1) For flat and windless courses, varying power caused a 0.5–0.7 second delay compared to a constant power
313 pacing strategy. However, a fast-starting strategy with a moderate start sprint shortened the finishing time by
314 about 1 second.

315 (2) Increasing power during uphill or headwind sections and decreasing power during downhill or tailwind

316 sections improved finishing times by 0.5–3.0 seconds in most cases. However, this strategy was ineffective for
317 downhill-then-uphill courses. Applying the opposite strategy in uphill-then-downhill scenarios worsened
318 finishing times significantly, by about 30 seconds.

319
320 The accuracy of commercial power meters is within 1–2%, and cycling computers display power in 1-watt
321 increments. Numerous factors such as minor course unevenness, temperature, humidity, and changes in wind
322 direction and speed can all affect finish time. Even small differences in clothing or body position on the day can
323 alter aerodynamic drag. Therefore, for the 10 km time trials, a constant power pacing strategy with a moderately
324 fast start is recommended. If there is one thing to avoid, it is reducing power on uphill sections.

325
326 For 1 km time trials, the findings are as follows:

327
328 (1) A linearly decreasing power pacing strategy yielded the best performance, improving finish times by 1.4
329 seconds on windless, flat courses.
330 (2) Variable power pacing strategies shortened finishing times by 2.2–4.2 seconds on windy or hilly courses,
331 except for the case of a tailwind followed by a headwind, where times worsened by 0.5–1.7 seconds.
332 (3) Power adjustments exceeding 10 W were possible and had a particularly large effect for courses with an initial
333 downhill followed by an uphill section.

334
335 Considering the above results, a variable power pacing strategy is recommended for a 1 km time trial. On a flat,
336 windless course, the linear tapering pacing strategy yields the best performance. If this is difficult to implement, a
337 two-step power pacing strategy can be adopted as an alternative. On a hilly course, power should be increased on
338 uphills and reduced on downhills. Unfortunately, the wind conditions investigated in this study are not fully realistic.
339 To achieve more realistic simulations, deceleration at corners should also be taken into account.

340
341 While considering exertion and acceleration in cycling time trial simulations is not novel, extending this approach
342 to more complex courses with multiple hills and corners will help develop practical pacing guidelines. Furthermore,
343 a device that displays current exertion and predicts exertion until the finish line could greatly assist cyclists in
344 optimizing their pacing if developed.

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349

350 **Conflict of interest**

351 The authors report there are no competing interests to declare.

352

353 **CRediT authorship contribution statement**

354 YF was responsible for conceptualization, data curation, methodology, supervision, validation, and writing –
355 review & editing. BA was responsible for data curation, formal analysis, investigation, software, visualization,
356 and writing – original draft. All authors have read and approved the final version of the manuscript and agreed
357 with the order of authorship.

358

359 **Declaration of generative AI and AI-assisted technologies in the writing process**

360 During the preparation of this work the authors used ChatGPT3.5 in order to improve their English writing. After
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367 **Statement of ethics**

368 This study does not involve human participants and therefore does not require IRB approval.

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402

403 Table 1 Parameters for calculation.

404	-----
405	M 70 kg
406	m 8.0 kg
407	m' 1.4 kg
408	ρ 1.20 kg/m ³ (1 atm., 293K, dry)
409	$C_D A$ 0.22 m ²
410	C_R 0.005
411	L 0.17 m
412	r_w 0.334 m (2.10 m circumference)
413	R_G 53 t/15 t
414	-----

415
416 Table 2 Windless flat 10 km time trial course (% change: percentage change in finishing time compared to the
417 constant power pacing strategy. *Italics* indicate slower cases, and **bold** indicates faster cases. This notation is used
418 consistently below.)

419	-----		
420	Case	Power (W)/lap time (s) for the first half	Power (W)/lap time (s) for the latter half
421			Time (s)/% change
422	-----		
423	<i>10DI</i>	252.2/441.80	273.4/416.89
424	10C	262.6/434.85	262.6/423.14
425	<i>10IDmax</i>	273.0/428.69	252.0/429.74
426	-----		

427
428 Table 3 Effects of a start sprint on a windless, flat 10 km time trial course

429	-----		
430	Case	Power for the start sprint (W)	Cruising power (W)
431			Time (s)/% change
432	10S-062.6	200	262.7
433	10S+037.4	300	262.4
434	10S+137.4	400	261.8
435	10S+237.4	500	261.0
436	-----		

437
438 Table 4 Effects of headwind and tailwind for a flat 10 km course

439	-----		
440	Case	Power (W)/lap time (s) for headwind	Power (W)/lap time (s) for tailwind
441			Time (s)/% change
442	-----		
443	<i>10HTDI</i>	257.5/775.21	269.1/283.71
444	10HTC	260.7/769.56	260.7/285.73
445	10HTIDmax	263.9/763.90	252.1/288.39
446	-----		

447
448 Table 5 Effects of tailwind and headwind on a flat 10 km course

449	-----		
450	Case	Power (W)/lap time (s) for tailwind	Power (W)/lap time (s) for headwind
451			Time (s)/% change
452	-----		
453	10THDImin	252.0/293.65	264.2/743.85
454	10THC	260.8/290.79	260.8/747.00
455	<i>10THID</i>	269.6/288.40	257.4/754.40
456	-----		

459 Table 6 Effects of uphill and downhill on a windless 10 km course
460

461 Case	462 Power (W)/lap time (s) 463 for uphill	464 Power (W)/lap time (s) 465 for downhill	466 Time (s)/% change
467 10UDDImin	468 252.0/1619.29	469 294.0/208.95	470 1828.24/1.68
471 10UDC	472 257.1/1587.20	473 257.1/210.79	474 1797.99
10UDID	257.8/1584.96	252.0/211.23	1796.19/−0.10

475 Table 7 Effects of downhill and uphill on a windless 10 km course
476

477 Case	478 Power (W)/lap time (s) 479 for downhill	480 Power (W)/lap time (s) 481 for uphill	482 Time (s)/% change
483 10DUDImin	484 252.0/212.23	485 258.0/1522.93	486 1735.16/0.01
487 10DUC	488 257.2/212.00	489 257.2/1522.92	490 1734.92
10DUID	262.4/211.64	256.5/1537.05	1748.69/0.79

491 Table 8 Windless, flat 1 km course
492

493 Case	494 Average power (W) 495 /lap time (s) of first half	496 Average power (W) 497 /laptime (s) of latter half	498 Time (s) /% change
499 IDI	500 276.8/52.587	501 419.7/37.645	502 90.232/3.6
503 1C	504 346.9/48.586	505 346.9/38.489	506 87.075
1IDmax	417.0/45.601	252.0/40.392	85.993/−1.2
425.8→252 (W)	382.4/46.243	295.5/39.461	85.704/−1.6

507 Table 9 Effects of headwind and tailwind on a flat 1 km course
508

509 Case	510 Power (W)/lap time (s) 511 for headwind	512 Power (W)/lap time (s) 513 for tailwind	514 Time (s)/% change
515 IHTDI	516 287.8/77.131	517 396.9/36.357	518 113.488/3.5
519 1HTC	520 329.1/71.915	521 329.1/37.690	522 109.605
1HTIDmax	370.4/67.725	252.0/39.718	107.443/−2.0

523 Table 10 Effects of tailwind and headwind on a flat 1 km course
524

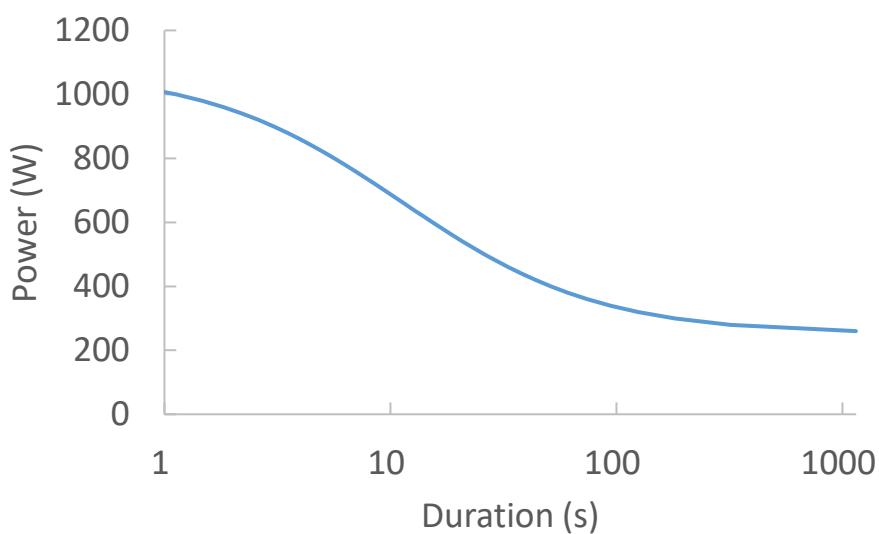
525 Case	526 Power (W)/lap time (s) 527 for tailwind	528 Power (W)/lap time (s) 529 for headwind	530 Time (s)/% change
531 ITHDImin	532 252.0/46.695	533 395.4/53.329	534 100.024/2.2
535 ITHDI−10%	536 303.6/43.926	537 361.7/54.386	538 98.312/0.5
539 1THC	540 337.3/42.452	541 337.3/55.395	542 97.847
1THID+10%	371.0/41.173	311.2/56.697	97.870/0.02

512 Table 12 Effects of uphill and downhill on a windless 1 km course
513

514 Case	515 Power (W)/lap time (s) 516 for uphill	517 Power (W)/lap time (s) 518 for downhill	519 Time (s)/% change
520 1UDDI	291.9/142.472	352.1/29.206	171.678/3.1
521 1UDC	304.4/136.485	304.4/29.621	166.485
522 1UDIDmax	316.9/132.202	252.0/30.119	162.321/-2.5

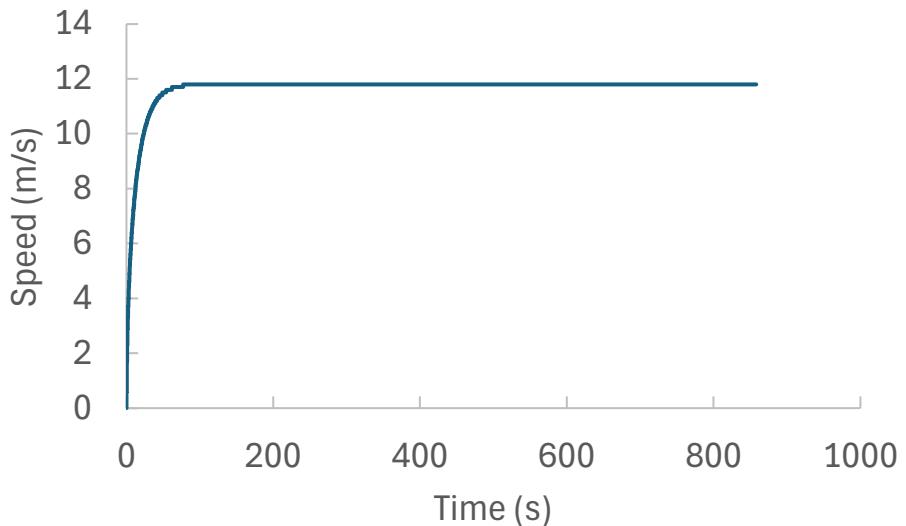
521 Table 13 Effects of downhill and uphill on a windless 1 km course
522

523 Case	524 Power (W)/lap time (s) 525 for downhill	526 Power (W)/lap time (s) 527 for uphill	528 Time (s)/% change
529 1DUDImin	252.0/31.530	355.2/78.461	109.991/-3.0
530 1DUDI-10%	293.9/30.991	340.0/80.256	111.247/-1.9
531 1DUC	326.5/30.608	326.5/82.826	113.434
	<i>1DUID+10%</i>	<i>359.2/30.250</i>	<i>115.917/2.2</i>



532

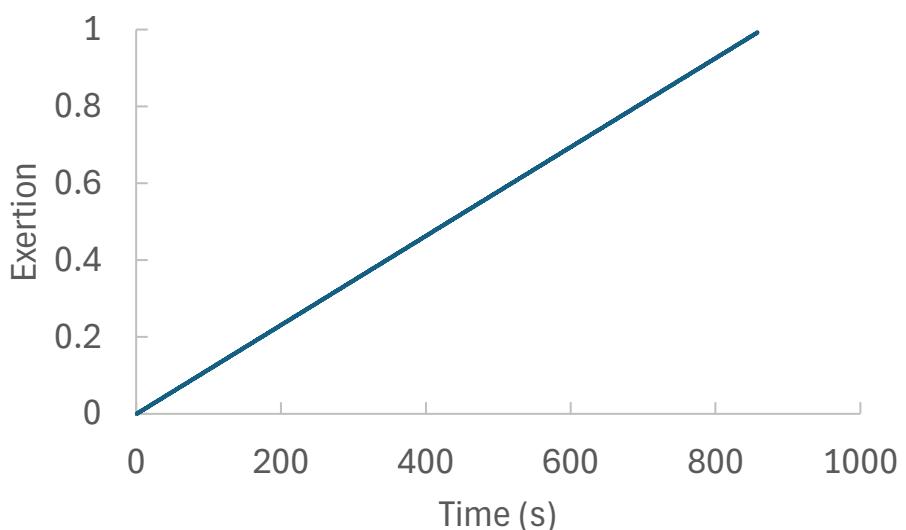
533 Fig. 1 Assumed peak power-time curve.
534



535

536

(a)



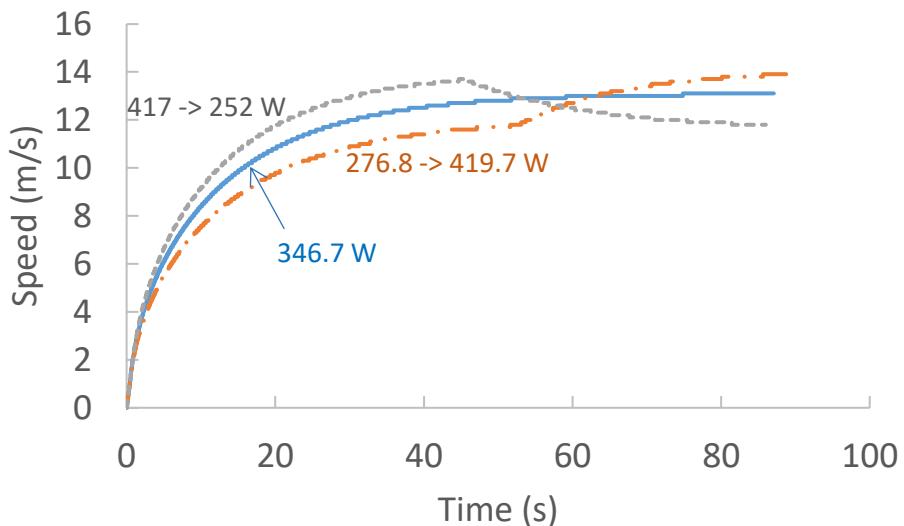
537

538

(b)

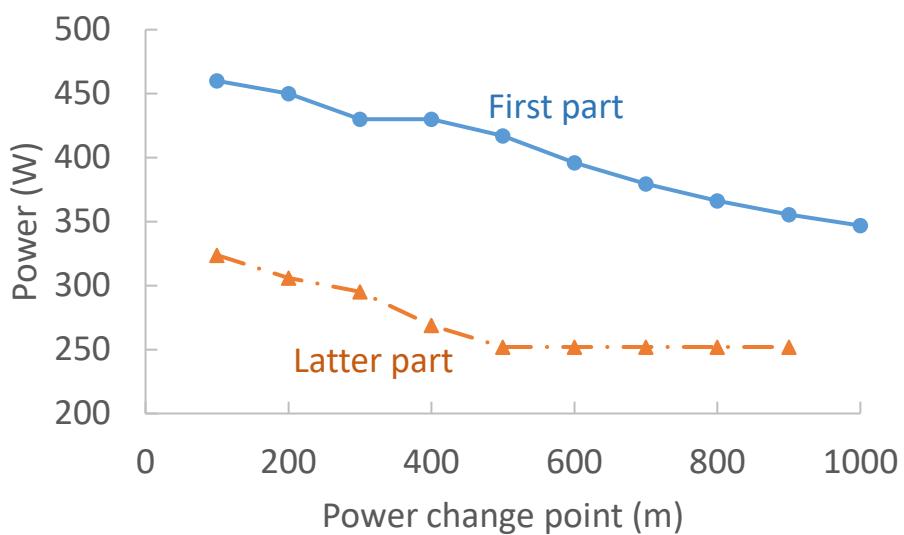
539 Fig. 2 Speed (a) and exertion (b) for the 10 km course (10C in Table 2).

540



541

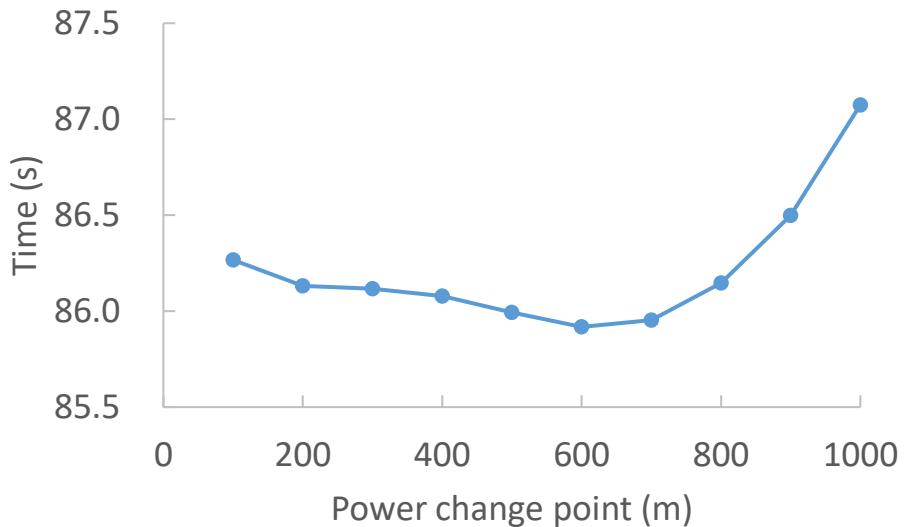
542 Fig. 3 Effect of power change on the windless flat 1 km course.



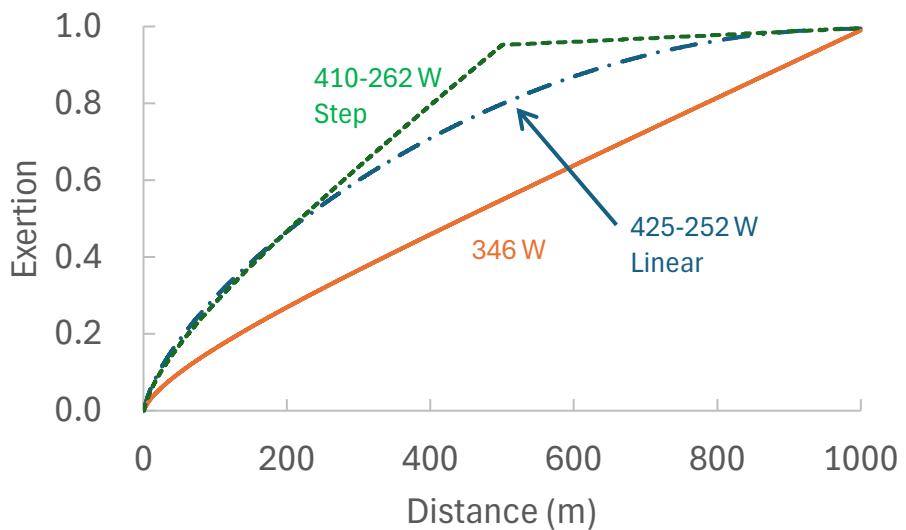
543

544 Fig. 4 Best combination of power levels for the windless and flat 1 km course.

545



546
547 Fig. 5 Effect of power change point on the finish time for the windless, flat 1000 m time trial.
548



549
550 Fig. 6 Exertion for constant power, step and linearly decreasing power cases.
551